

Video  
903  
(5:05)

**Simple Harmonic Motion**

restoring force:

When a stable system at equilibrium is tweaked, often some kind of restoring force naturally kicks in.



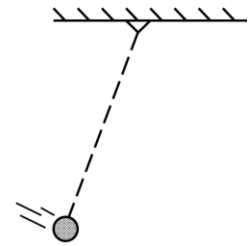
In simple harmonic motion (SHM), the restoring force is directly proportional to the displacement from equilibrium, i.e.,

As  $\Delta x \uparrow$ ,  $F \downarrow$  . As  $\Delta x \downarrow$ ,  $F \uparrow$  . When  $\Delta x = 0$ ,  $F = 0$

We will learn about two cases that exhibit (or nearly so) SHM.



mass-spring system



pendulum

amplitude:

For m-s systems:

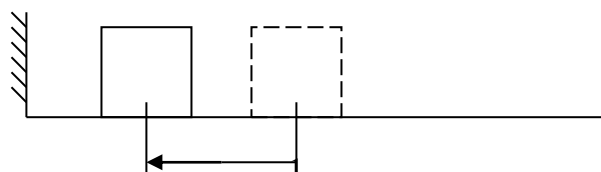
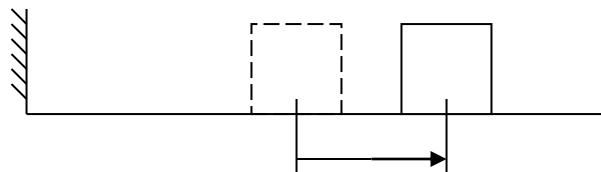
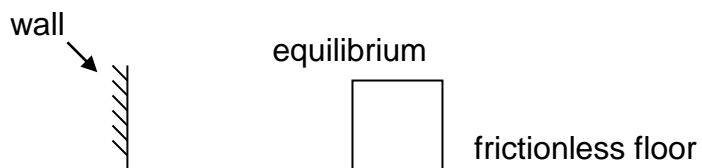
- symbolized A
- measured in

For pendulums:

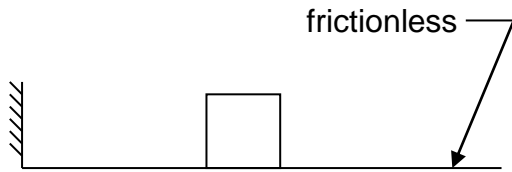
- symbolized  $\theta$
- measured in

**Mass-Spring System**

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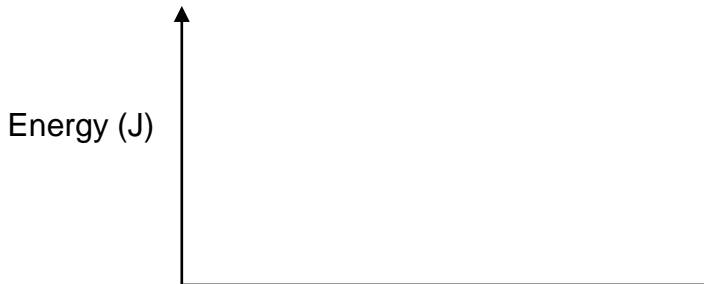
## Mass-Spring System



$\Delta x_{\max}$  is better known as the...

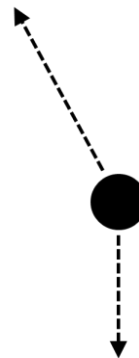
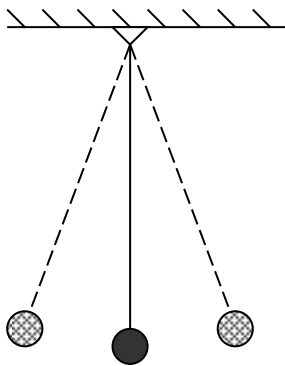
At that point, we also have maximum...

### Energy of a Mass-Spring System



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## Pendulum



$\theta$ (deg)	$\sin \theta$	$\theta$ (rad)
0		
5		
10		
15		
20		
25		

### Energy of a Simple Pendulum





period,  $T$ :



frequency,  $f$ :

For mass-spring systems:

$m$  = mass (kg)

$k$  = spring constant (N/m)



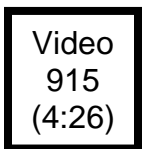
A 5.5 kg cat is attached to a fixed horizontal spring of stiffness 22.8 N/m and is set in motion on a frictionless surface. Find the period of motion of...

...the cat.



...a 120 g mouse, with the same spring and surface.

What stiffness must a spring have so that the period of the mouse's motion is the same as that of the cat?



A 1645 kg car carries two passengers with masses 75 kg and 86 kg. The car has four shock absorbers, each with a spring constant of  $1.7 \times 10^4$  N/m. Find the freq. of the vehicle's motion after it hits a pothole.



For simple pendulums:

Period  $T$  is independent of...



EX. The period of a pendulum is 5.2 s. Find...

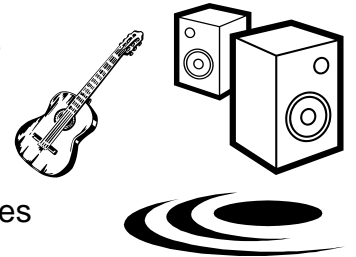
A. ...its length

B. ...the mass of the bob

EX. On Io, a moon of Jupiter, a 0.87 m pendulum has a period of 8.74 s. What is g on Io?

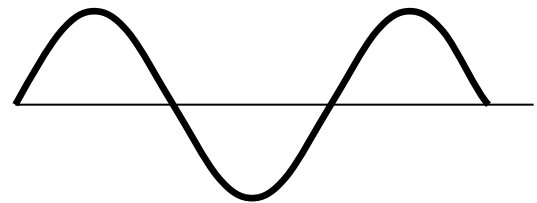
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**Waves** → vibrations moving through space and time



medium: the matter through which the energy of mechanical waves moves

transverse waves: particles of medium move  $\perp$   
to direction of wave travel



longitudinal (compressional) wave: particles of  
medium move  $\parallel$  to direction of wave travel



pulse wave:  
vs. periodic wave:

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For mechanical waves:



If A doubles, energy...

If A triples, energy...

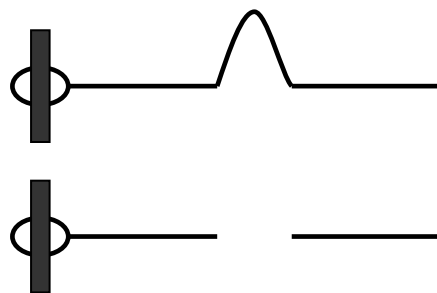
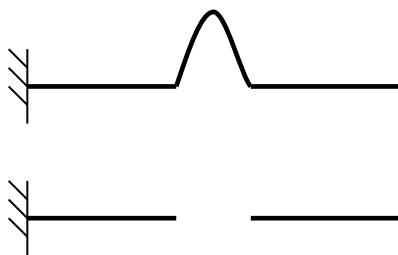
If A drops to, say, 35% of the original level, energy...

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**Wave Reflection**

fixed boundary

vs. free boundary



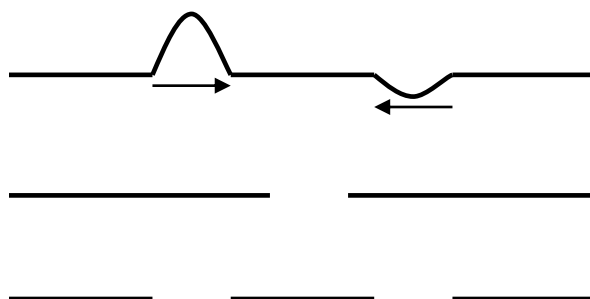
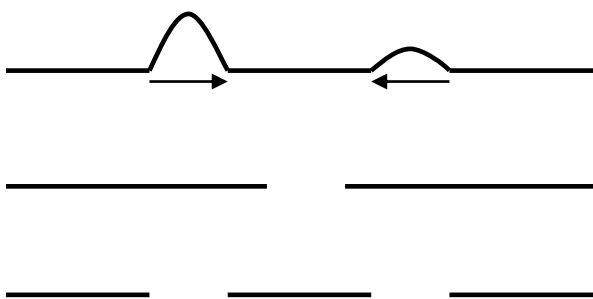
**Wave Interference**

Two waves (unlike two objects) can occupy the same place at the same time.

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constructive interference:

destructive interference:



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**Wave Velocity**

Equation:

$v$  (m/s);  $f$  (Hz);  $\lambda$  (m)

EX. A wave of wavelength 8.5 m washes past a boat at anchor every 4.75 s. Find wave's velocity.



The speed of any mechanical wave depends **only** on the properties of the medium through which it travels.

e.g.,



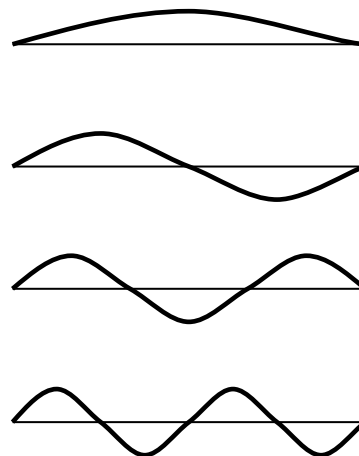
The speed of sound in air is related to the air temperature:

## Standing Waves

Incident and reflected waves interfere to produce an unchanging wave pattern. Antinodes have a max. amplitude, while nodes have zero amplitude.

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Standing waves are most easily visualized on a string, where nodes remain motionless and antinodes go from max. (+) to max. (-) displacement.



wavelength of the  $n^{\text{th}}$  harmonic on a string:

EX. Waves travel along a 96.1 cm guitar string at 492 m/s. Find fundamental frequency of string.

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(4:06)



Find the frequency of the 5<sup>th</sup> harmonic.

frequency of the  $n^{\text{th}}$  harmonic:

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(6:35)

### Standing Waves in Open Tubes

wavelength of the  $n^{\text{th}}$  harmonic of an open tube:



### Closed Tubes

wavelength of the  $n^{\text{th}}$  harmonic of a closed tube:



EX. Find fundamental freq. for an open tube of length 1.24 m. Air temp. is 20.0°C.

EX. Find fundamental freq. for a closed tube of length 1.24 m. Air temp. is 20.0°C.

doubling (or halving) of frequency =

100 Hz  $\longleftrightarrow$  200 Hz  $\longleftrightarrow$  400 Hz  $\longleftrightarrow$  800 Hz

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Sound

compression:

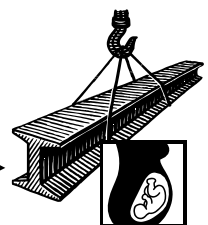
rarefaction:



← 20 Hz



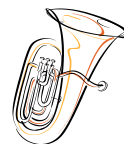
20,000 Hz →



Fundamental frequency determines pitch.

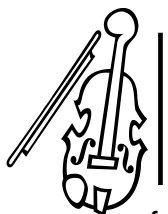


high f =



low f =

The # and intensity of an instrument's harmonics give it its unique sound quality, or \_\_\_\_\_.



f<sub>1</sub> f<sub>2</sub> f<sub>3</sub> f<sub>4</sub>



f<sub>1</sub> f<sub>2</sub> f<sub>3</sub> f<sub>4</sub>



f<sub>1</sub> f<sub>2</sub> f<sub>3</sub> f<sub>4</sub>



f<sub>1</sub> f<sub>2</sub> f<sub>3</sub> f<sub>4</sub>

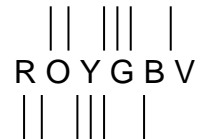
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### The Doppler Effect

Relative motion between wave source and observer causes a change in the \_\_\_\_\_ frequency.



Other examples of the Doppler effect:

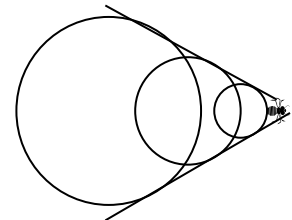
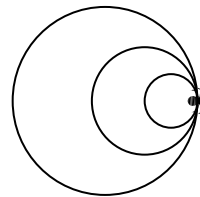
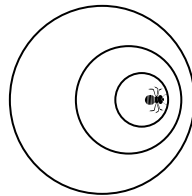
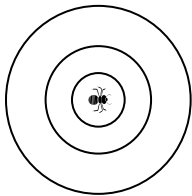


Sun

most stars

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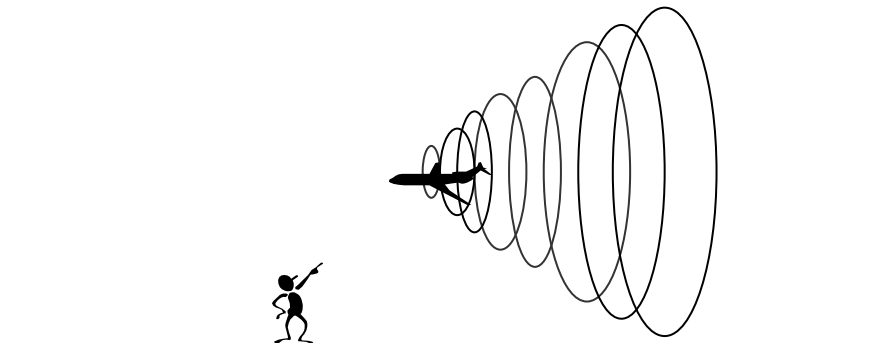
### Traveling Very Fast



supersonic: "faster than sound" (vs. subsonic)

shock wave:

sonic boom:





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(3:30)

### Sound Intensity

Equation:



EX. If a piano's power output is 0.302 W, find the sound intensity at a distance of...

A. ...1.0 m

B. ...2.0 m

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Intensity is related to volume (or relative intensity):

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-- measured in decibels (dB)

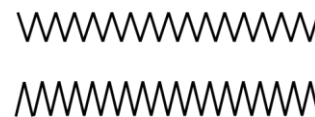
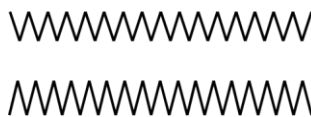
A difference of 10 dB changes the sound intensity by a factor of 10 and the volume by a factor of 2.

50 dB vs. 40 dB

60 dB vs. 90 dB

**Beats** → alternating loud-and-soft sounds resulting from interference between two slightly-different frequencies

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(5:16)



Equation:

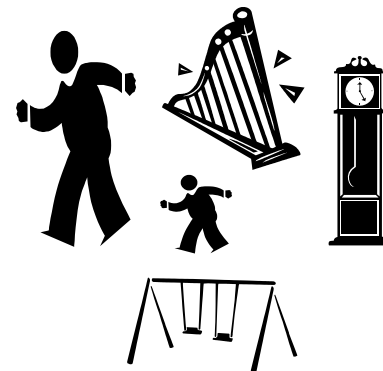
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(5:50)

### Forced Vibrations and Resonance

natural frequency:

forced vibration:

resonance:



-- result of resonance =

Examples:

